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DEPARTMENT OF COMPUTER SCIENCE ENGINEERING



MACHINE LEARNING  
Combining Inductive and Analytical Learning  
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# Combining Inductive and Analytical Learning

- Why combine inductive and analytical learning?
- KBANN: prior knowledge to initialize the hypothesis
- TangentProp, EBNN: prior knowledge alters search objective
- FOCL: prior knowledge alters search operators

# Inductive and Analytical Learning

## Inductive learning

Hypothesis fits data

Statistical inference

Requires little prior knowledge

Syntactic inductive bias

## Analytical learning

Hypothesis fits domain theory

Deductive inference

Learns from scarce data

Bias is domain theory

# What We Would Like

Inductive learning

Analytical learning

Plentiful data

Scarce data

No prior knowledge

Perfect prior knowledge

- General purpose learning method:
- No domain theory → learn as well as inductive methods
- Perfect domain theory → learn as well as PROLOG-EBG
- Accommodate arbitrary and unknown errors in domain theory
- Accommodate arbitrary and unknown errors in training data

# Domain Theory

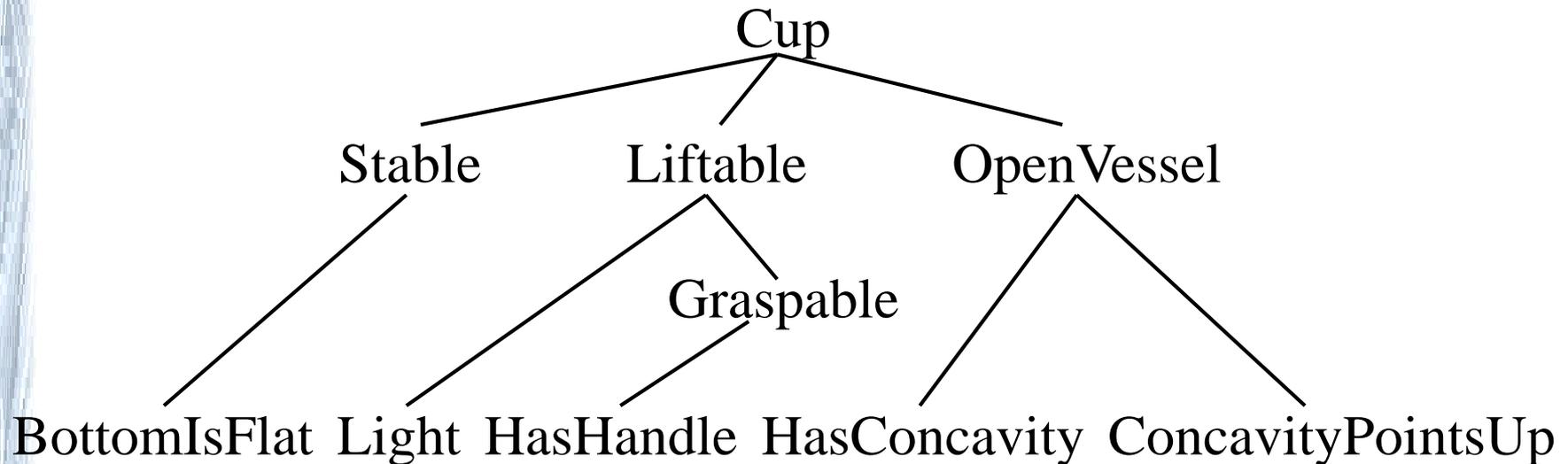
Cup ← Stable, Lifiable, OpenVessel

Stable ← BottomIsFlat

Lifiable ← Graspable, Light

Graspable ← HasHandle

OpenVessel ← HasConcavity, ConcavityPointsUp



# Training Examples

	Cups				Non-Cups					
BottomIsFlat	✓	✓	✓	✓	✓	✓	✓			✓
ConcavityPointsUp	✓	✓	✓	✓	✓		✓	✓		
Expensive	✓		✓				✓		✓	
Fragile	✓	✓			✓	✓		✓		✓
HandleOnTop					✓		✓			
HandleOnSide	✓			✓					✓	
HasConcavity	✓	✓	✓	✓	✓		✓	✓	✓	✓
HasHandle	✓			✓	✓		✓		✓	
Light	✓	✓	✓	✓	✓	✓	✓		✓	
MadeOfCeramic	✓				✓		✓	✓		
MadeOfPaper				✓					✓	
MadeOfStyroForm		✓	✓			✓				✓

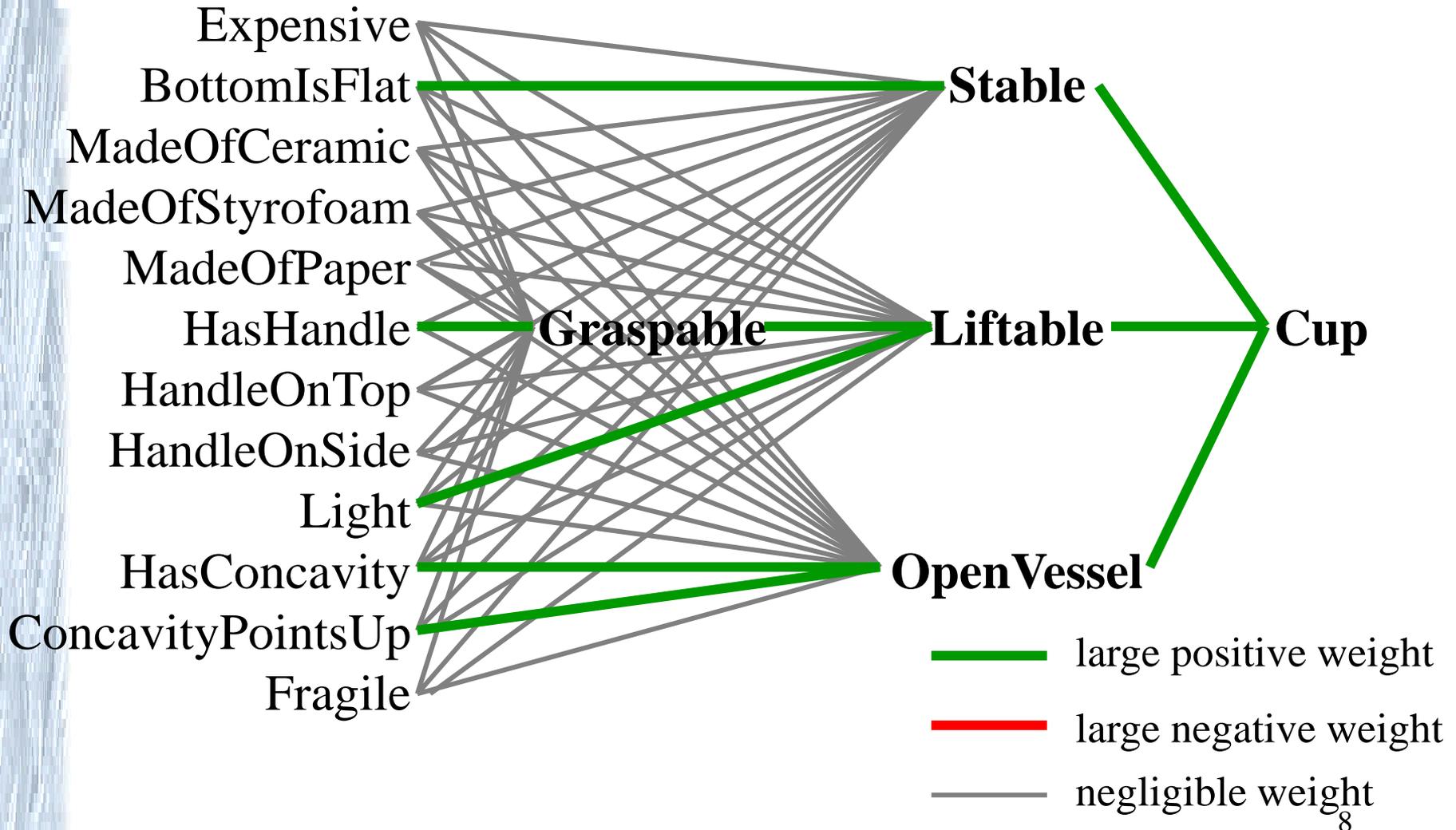
# KBANN

Knowledge Based Artificial Neural Networks

KBANN (data  $D$ , domain theory  $B$ )

1. Create a feedforward network  $h$  equivalent to  $B$
2. Use BACKPROP to tune  $h$  to fit  $D$

# Neural Net Equivalent to Domain Theory



## Creating Network Equivalent to Domain Theory

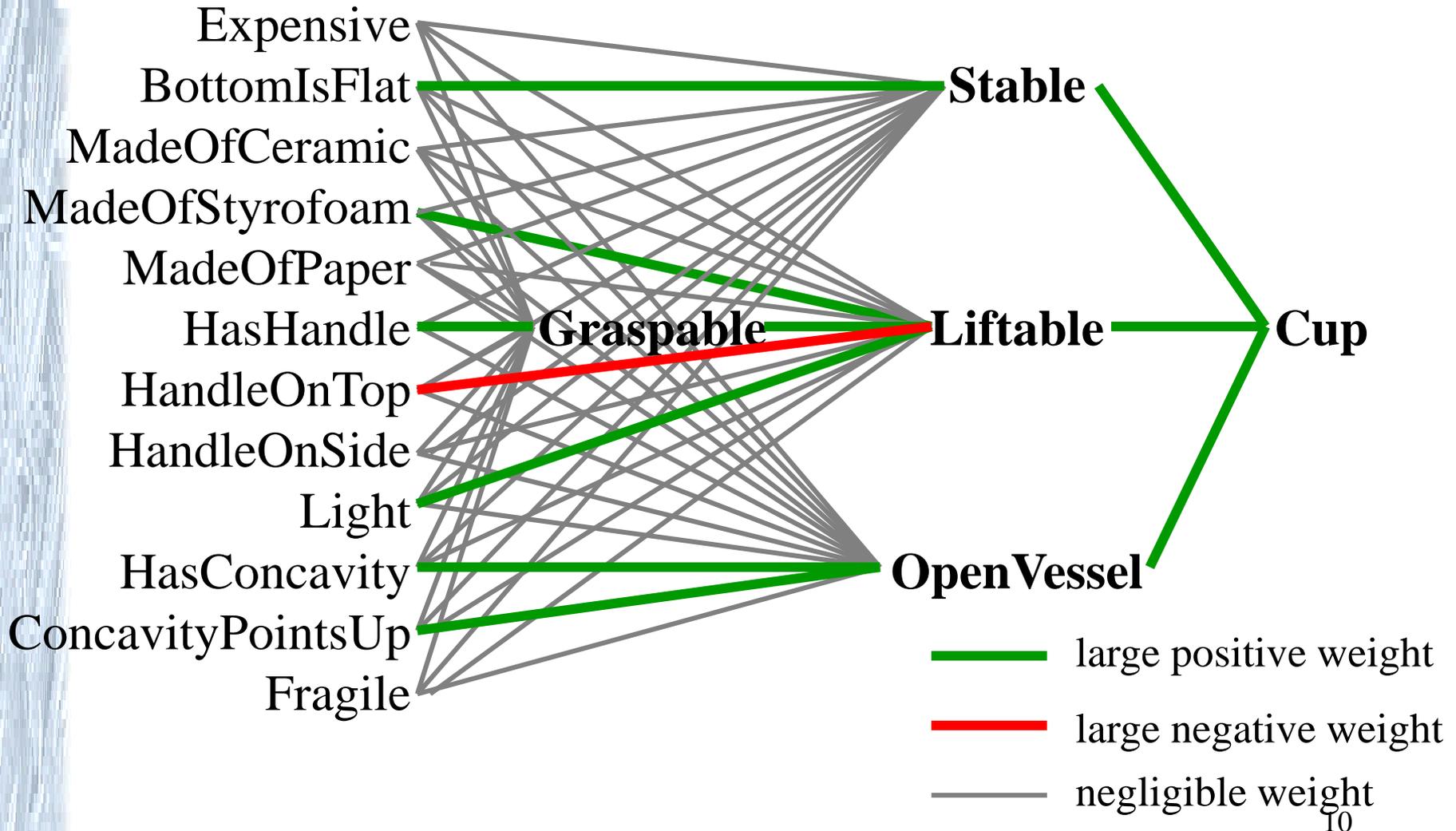
Create one unit per horn clause rule (an AND unit)

- Connect unit inputs to corresponding clause antecedents
- For each non-negated antecedent, corresponding input weight  $w \leftarrow W$ , where  $W$  is some constant
- For each negated antecedent, weight  $w \leftarrow -W$
- Threshold weight  $w_0 \leftarrow -(n - .5) W$ , where  $n$  is number of non-negated antecedents

Finally, add additional connections with near-zero weights

*Liftable*  $\leftarrow$  *Graspable*,  $\neg$ *Heavy*

# Result of Refining the Network



# KBANN Results

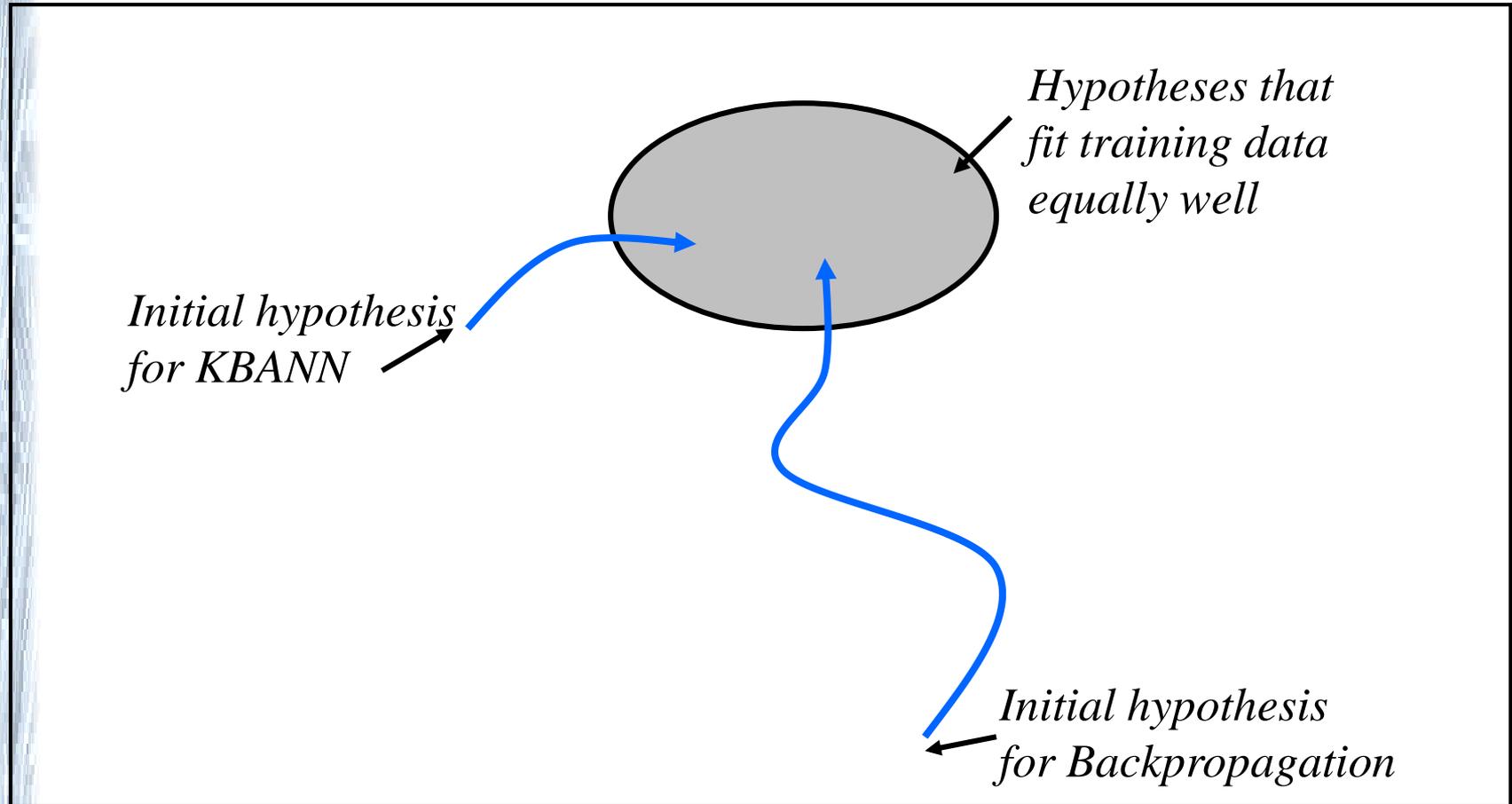
Classifying promoter regions in DNA (leave one out testing):

- Backpropagation: error rate 8/106
- KBANN: 4/106

Similar improvements on other classification, control tasks.

# Hypothesis Space Search in KBANN

## Hypothesis Space



# EBNN

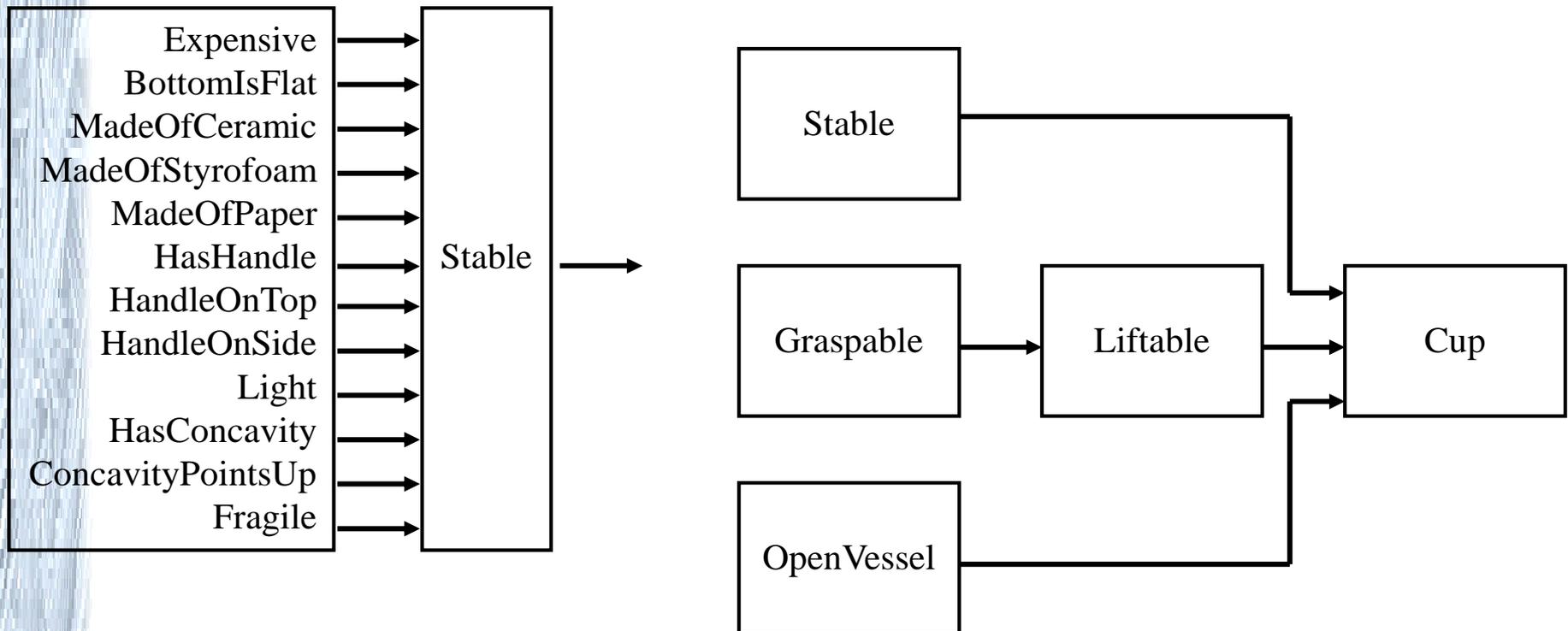
## Explanation Based Neural Network

Key idea:

- Previously learned approximate domain theory
- Domain theory represented by collection of neural networks
- Learn target function as another neural network

# Explanation in Terms of Domain Theory

Prior learned networks for useful concepts combined into a single target network



# TargetProp

Assume  $x$ ,  $f(x)$  and  $\left. \frac{\partial f(x)}{\partial x} \right|_{x_i}$  provided as input

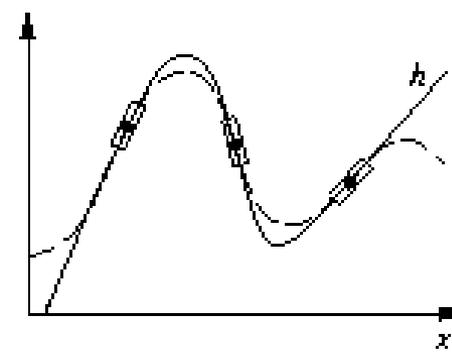
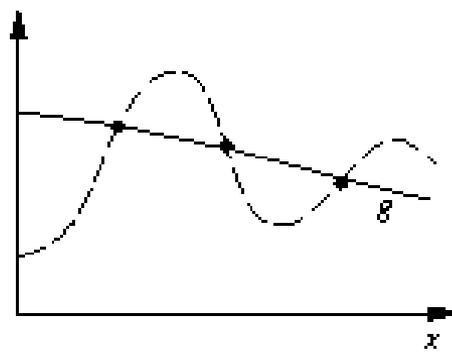
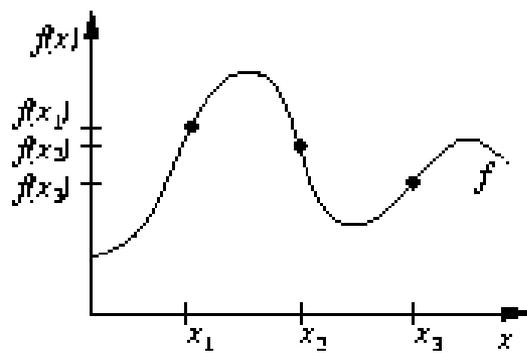
Modified objective for gradient descent :

$$E = \sum_i \left[ (f(x_i) - \hat{f}(x_i))^2 + \mu_i \sum_j \left( \frac{\partial A(x)}{\partial x^j} - \frac{\partial \hat{f}(x)}{\partial x^j} \right)^2 \Big|_{(x=x_i)} \right]$$

where

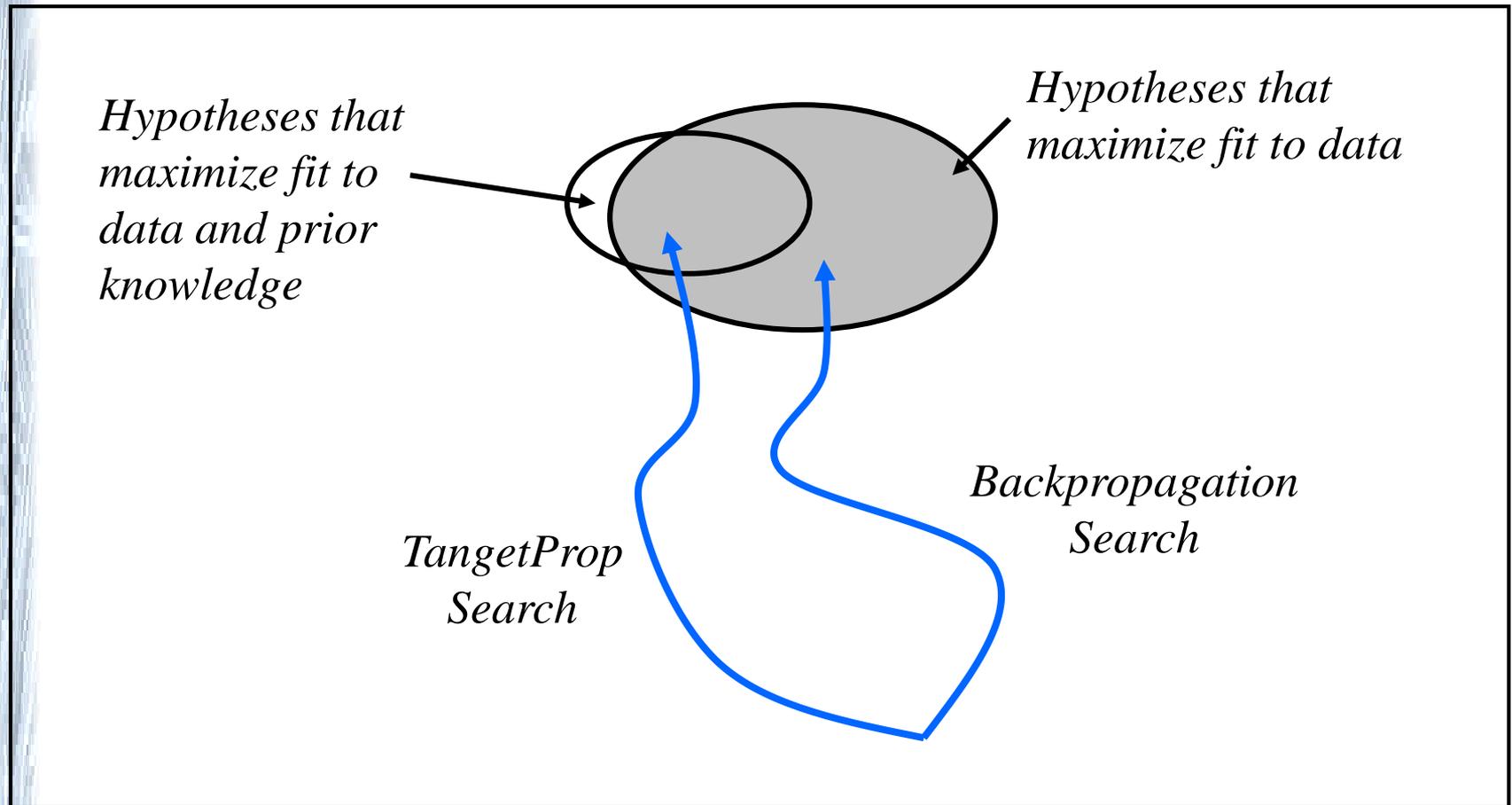
$$\mu_i \equiv 1 - \frac{|A(x_i) - f(x_i)|}{c}$$

- $f(x)$  is target function
- $\hat{f}(x)$  is neural net approximation to  $f(x)$
- $A(x)$  is domain theory approximation to  $f(x)$



# Hypothesis Space Search in TangentProp

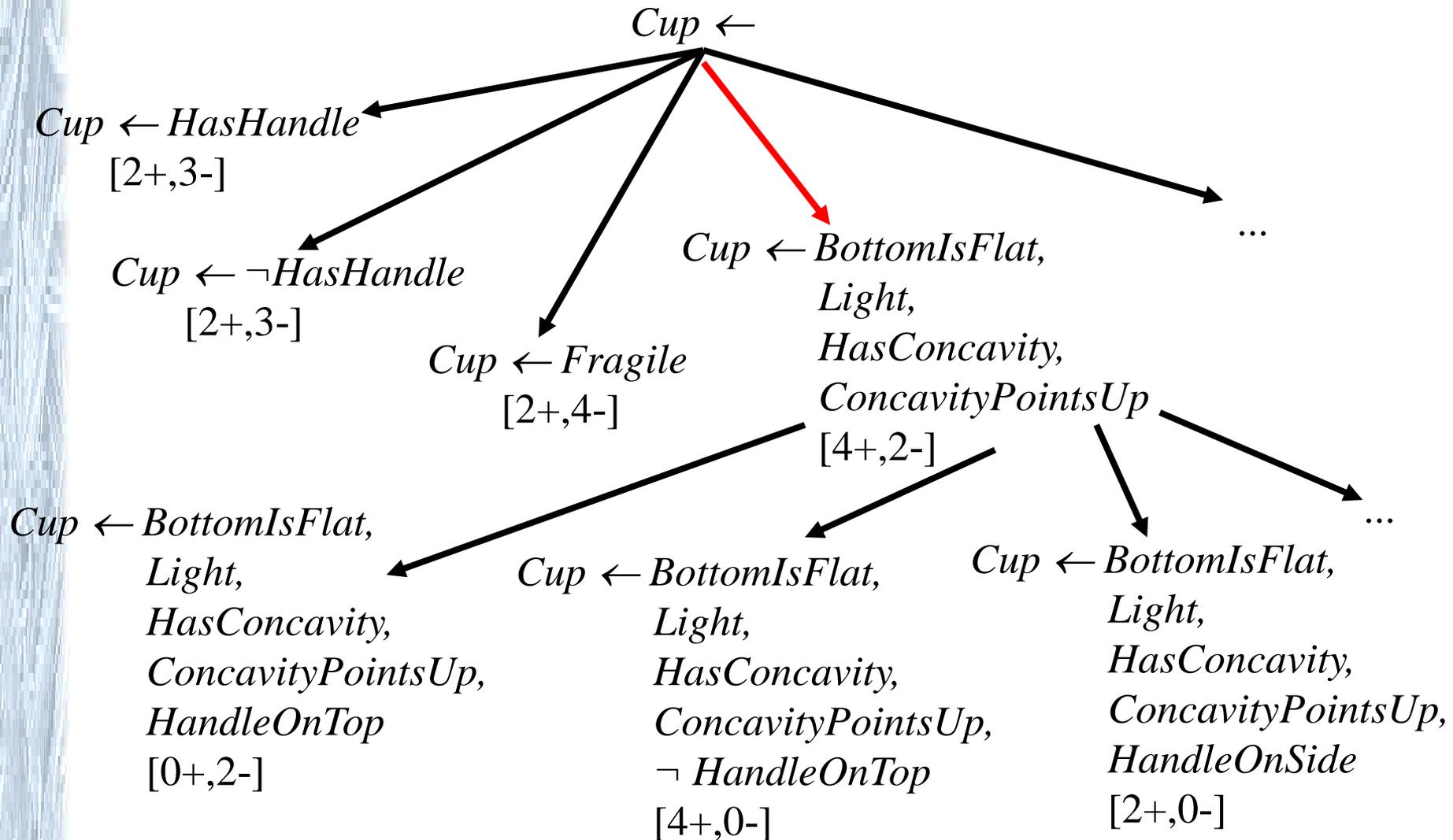
## Hypothesis Space



# FOCL

- Adaptation of FOIL that uses domain theory
- When adding a literal to a rule, not only consider adding single terms, but also think about adding terms from domain theory
- May also prune specializations generated

# Search in FOCL



# FOCL Results

Recognizing legal chess endgame positions:

- 30 positive, 30 negative examples
- FOIL: 86%
- FOCL: 94% (using domain theory with 76% accuracy)

NYNEX telephone network diagnosis

- 500 training examples
- FOIL: 90%
- FOCL: 98% (using domain theory with 95% accuracy)